



Homework1

Due date: Monday, January 22, 2007

Using the data below, prepare the following number distributions. The first row of the Table has been completed as a guide. Use a spreadsheet or graph paper.

1. Plot a simple histogram ( $n_N$  vs.  $D_p$ ; actually column 2, the mean of the size interval).
2. Prepare a semi-logarithmic plot of the same data ( $n_N^e$  vs.  $\ln D_p$ ). Calculate  $\Delta \ln D_p$  from the first column.
3. Prepare a cumulative distribution plot (% less than the indicated  $D_p$  vs.  $D_p$ )
4. Prepare a log-normal plot using the attached log-probability paper ( $D_p$  vs. percent-less-than-the-indicated  $D_p$ ).
5. Recognizing that  $\bar{D}_{pg} = D_{\text{median}}$  and that  $\sigma_g = D_p^{84.1\%} / \bar{D}_{pg}$ , read off  $\bar{D}_{pg}$  and  $\sigma_g$  from your plot (e.g., Figure 4.12).
6. Use these parameters to calculate a continuous log-normal distribution curve and superimpose the curve onto the discrete raw data to check the goodness of fit (see Fig. 14.2 for example).

| Size Interval ( $\mu\text{m}$ ) | Geometric Mean Diam., $\bar{D}_{pg}$ ( $\mu\text{m}$ ) | Concentration within Interval, $\Delta N$ ( $\#/ \text{cm}^3$ ) | $n(D_p) = dN/d(D_p)$ ( $\#/ \text{cm}^3 / \mu\text{m}$ ) | $\ln D_p$ | $\Delta \ln D_p$ | $n(\ln D_p) = dN/d(\ln D_p)$ ( $\#/ \text{cm}^3$ ) | Cum. % less than | $n(\ln D_p)$ (calculated from eq 1 below) |
|---------------------------------|--|---|--|-----------|------------------|--|------------------|---|
| 0.1-0.2                         | 0.14   | 50  | 500  | -1.956    | 0.693            | 72   | .99              | 207.8                                     |
| 0.2-0.4                         | 0.28   | 460   |  |           |                  |  |                  |   |
| 0.4-0.7                         | 0.53   | 1050  |  |           |                  |  |                  |   |
| 0.7-1.0                         | 0.84   | 980   |  |           |                  |  |                  |   |
| 1-2                             | 1.41   | 1700  |  |           |                  |  |                  |   |
| 2-4                             | 2.83   | 680   |  |           |                  |  |                  |   |
| 4-7                             | 5.29   | 100   |  |           |                  |  |                  |   |
| 7-10                            | 8.37   | 10  |  |           |                  |  |                  |   |
| 10-20                           | 14.1   | 2   |  |           |                  |  |                  |   |

$$n_N(\ln D_p) = \frac{dN}{d \ln D_p} = \frac{N}{\sqrt{2\pi} \ln \sigma_g} \exp\left(-\frac{(\ln D_p - \ln \bar{D}_{pg})^2}{2 \ln^2 \sigma_g}\right) \quad \text{eq 1.}$$

Graduate Students (and Undergraduates for extra Credit)

Do Q 4.5.

